

SCHOOL OF FINANCE AND APPLIED ECONOMICS BBS Financial Economics, BBS Actuarial Science & BBS Finance END OF SEMESTER EXAMINATION BSA 2205: ECONOMETRICS II

DATE: 10th November 2016 TIME: 2 Hours

INSTRUCTIONS

- 1) Answer question one and any other two questions
- 2) Question one is compulsory and carries 30 marks
- 3) All other questions carry 20 marks each

Question 1 (30 marks)

Briefly discuss the following as applied in econometrics (6 marks each):

- (i) The concept of unbiasedness of parameter estimates
- (ii) The relevance of the Gauss-Markov theorem
- (iii) Method of Moments estimation
- (iv) Realistic Solutions to Multi-collinearity problem
- (v) The limitation of using Least squares to estimate a linear probability models

Question 2 (20 marks)

- a) Clearly demonstrate that Instrumental variable and Ordinary Least Squares estimation are special cases of method of moments modeling technique (be *sure to indicate their respective othorgonality conditions in your responses*). (10 marks)
- b) Consider the following time series model:

$$y_t = \beta_0 + \beta_1 x_{1t} + \beta_2 x_{2t} + \varepsilon_t$$

Where y_t is some outcome variable of interest, and x_{1t} and x_{2t} are strictly exogenous explanatory variables. Clearly, describe how one would test for Serial Correlation in the residual term ε_t using Breusch Godfrey Test? (10 marks)

Question 3 (20 marks)

- a) Discuss three merits and three demerits of maximum likelihood estimation (6 marks)
- b) Assume a normal distribution of errors in the model $Y = X\beta + \varepsilon$, where Y is the dependent variable, X a vector of independent variables, β is a vector of coefficients and ε is the error term. Using this information, show that error variances generated from Maximum Likelihood Estimation is lower than that generated by Ordinary Least Squares (OLS) estimation (use the unbiased estimate for error variance from OLS given by: $\delta^2 = \frac{1}{n-k} \sum (Y X\beta)'(Y X\beta) \). \ \ (\textbf{10 marks})$

c) Based on your results in (b) above, derive the variance of β (*Hint. Use the information matrix*). (4 marks)

Question 4 (20 marks)

- a) Discuss Heteroskedasticity, its sources and consequences in econometrics (6 marks)
- b) Outline a step by step process of how you would test for Heteroscedasticity using *White* test. Assume that heteroskedasticity is confirmed present, enlist at least two approaches that one can use to solve the problem (*consider the case where the form of Heteroscedasticity is known and when it is not known*) (**7 marks**)
- c) Discuss salient features of Generalized Method of Moments (6 marks)

Question 5 (20 marks)

- a) A second year student of Financial Economics at Strathmore University discovered after conducting regression using time series data of the model $y_t = \beta_0 + \beta_1 x_t + e_t$ that the variance of errors was not constant, but given by the expression $\delta^2 x^2_t$. Use the information to answer the following questions:
 - (i) Clearly outline how the student should go about estimations using Generalized Least Squares estimation technique. (7 marks)
 - (ii) In addition, prove that the approach makes the variance of the errors constant and equal to δ^2 . (3 marks)
- b) Consider a hypothetical function describing a distribution of x:

$$f(x) = \phi x^{\phi - 1}$$
 where $0 \le x \le 1$

Derive the maximum likelihood estimate for ϕ (10 marks)

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