

#### STRATHMORE INSTITUTE

#### **DIPLOMLOMA IN BUSINESS MANAGEMENT**

#### DIPLOMA IN INTERNATIONAL RELATIONS

#### DIPLOMA IN JOURNALISM AND NEW MEDIA

#### DIPLOMA IN BUSINESS CREATION AND ENTREPRENEURSHIP

#### **END OF SEMESTER EXAMINATION**

#### DBM 1204/ DIR1202 /DE 1105/ DJNM1202

#### **BUSINESS MATHEMATICS**

**DATE:** Friday, 14<sup>th</sup> April, 2023

Time: 2 Hours

## **Instructions**

1. This examination consists of **FIVE** questions.

- 2. Answer Question ONE (COMPULSORY) and any other TWO questions.
- 3. Do not write on the question paper.

## **QUESTION ONE [30 MARKS]**

a) Identify each of the following types of matrices:

i. 
$$W = \begin{bmatrix} 3 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$
ii. 
$$X = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$
iii. 
$$W = \begin{bmatrix} 4 & 0 & 0 \\ 0 & 8 & 0 \\ 0 & 0 & 2 \end{bmatrix}$$
iv. 
$$Z = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

[4 Marks]

b) Solve the following simultaneous equation:

$$4x + 5y = 11$$
  
 $10x + 3y = 18$  [4 Marks]

c) Without using mathematical tables, solve for x in the equation.

$$9^{(2x-1/4)} \times 27^{(x-1/2)} = 729^{(x+1/3)}$$
 [4 Marks]

d) Find the sum of all the numbers between 4 and 208 which are exactly divisible by 2.

[5 Marks]

- e) There are 30 houses on a street. 16 of the houses have burglar alarm, 22 have a smoke alarm, and 10 houses have both a burglar alarm and smoke alarm.
  - i. Draw this information on a Venn diagram. [3 Marks]
  - ii. How many houses have a burglar alarm but not a smoke alarm? [2 Marks]
  - iii. How many houses have either a burglar alarm or smoke alarm? [2 Marks]
- f) Simplify

$$\frac{\log 27 - \frac{1}{2}\log 9}{\log 81 + \frac{1}{2}\log 9}$$
 [3 Marks]

g) Determine the mean, mode and median for the following data: 3, 5, 8, 9, 3

[3 Marks]

## **QUESTION TWO [15 MARKS]**

- a) List the elements of the following sets
  - i.  $A = \{x : x \in \mathbb{N}, 3 < x < 6\}$  [1 Mark] ii.  $B = \{x : x \in \mathbb{N}, x^2 + 1 = 10\}$  [1 Mark]

iii.  $C = \{x : x \in \mathbb{N}, 7 + x = 4\}$  [1 Mark]

- b) A slaughter house bought goats and bulls at *Ksh.* 1, 200 and *Ksh.*15,000 each. They paid a total bill of *Ksh.* 135,000. If they double the number of goats and three bulls less, they would have saved *Ksh.* 15,000.
  - i. By using matrix method, determine the number of goats and bulls that were bought. [8 Marks]
  - ii. The slaughter house sold the animals at a profit of 25% per goat and 30% per bull. Determine the amount of profit made. [4 Marks]

# **QUESTION THREE [15 MARKS]**

The table below shows the lengths in centimetres of 40 steel rods in a workshop.

Length in cm	32 - 34	35-37	38-40	41-43	44 – 46	47 – 49
Frequency	6	5	10	12	4	3

a) Draw a histogram.

[3 Marks]

b) Determine the:

i.	Mode
ii.	Median

[3 Marks] [4 Marks]

iii. Mean [5 Marks]

# **QUESTION FOUR [15 MARKS]**

a) Given that  $\begin{pmatrix} 2-a & -3 \\ -5 & 6+b \end{pmatrix} = \begin{pmatrix} -2 & -3 \\ -5 & 16 \end{pmatrix}$ . Determine the values of a and b.

[2 Marks]

b) Given the matrices  $A = \begin{pmatrix} 1 & 0 & 1 \\ 2 & -2 & 1 \\ 1 & 2 & 1 \end{pmatrix}$  and  $B = \begin{pmatrix} -2 & 1 & 1 \\ 3 & 0 & 1 \\ 1 & 2 & 1 \end{pmatrix}$ , determine AB - 4A + 3B.

[6 Marks]

c) Solve the following equation:

$$x^2 + 6x + 5 = 0$$

[4 Marks]

d) Sales for a new magazine are expected to grow according the equation

$$S = 200,000 \left(1 - e^{-0.05t}\right),\,$$

 $S = 200,000(1 - e^{-0.05t})$ , where t is given in weeks.

Calculate the number of magazines sold after 20 weeks.

[3 Marks]

# **QUESTION FIVE [15 MARKS]**

- a) Let  $U = \{ whole numbers from 1 to 15 \}$ ,  $A = \{ factors of 12 \}$  and  $B = \{even \ numbers \ less \ than \ 15\}$ 
  - List the elements of A and B. I.

[2 Marks]

II. Find:

i. 
$$A \cap B$$

[2 Marks]

ii. 
$$A \cup B$$

[2 Marks]

iii. 
$$A - B$$

[2 Marks]

iv. 
$$n(A^C)$$

[2 Marks]

b) Solve for x in the equation: 
$$\log(3x+4) - \log(3-x) = 1$$

[5 Marks]

**END**